

Digital Circuits

ECS 371

Dr. Prapun Suksompong

prapun@siit.tu.ac.th

Lecture 11

Office Hours:

BKD 3601-7

Monday 9:00-10:30, 1:30-3:30

Tuesday 10:30-11:30

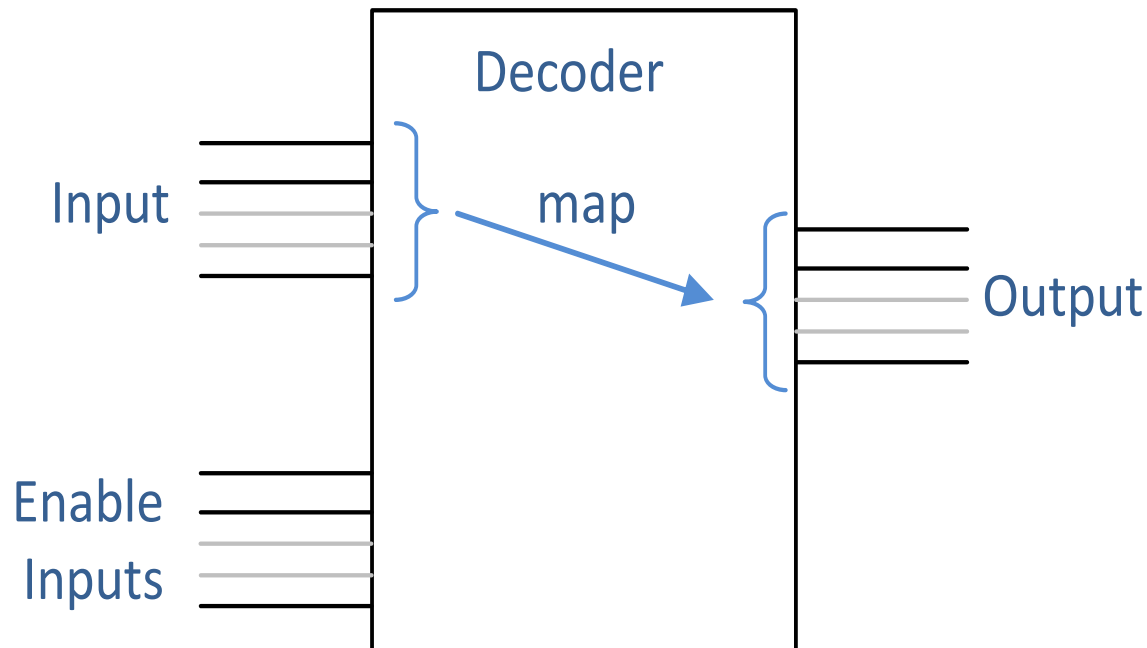
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Signals and their Active Levels

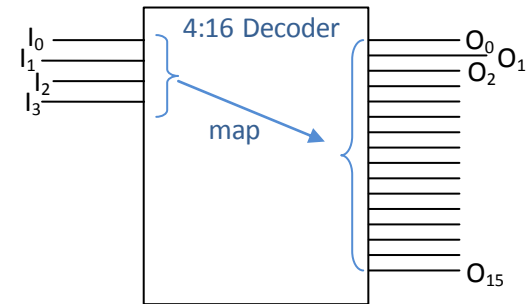
- Each input and output in a logic circuit should have a descriptive alpha-numeric label, the signal's name.
- A signal is **active high** if it performs the named action or denotes the named condition when it is HIGH (H) or 1.
- A signal is **active low** if it performs the named action or denotes the named condition when it is LOW (L) or 0.
- If not specified, assume active-high signal.
- A signal is said to be **asserted** when it is at its active level.
- A signal is said to be **negated** (or, sometimes, **deasserted**) when it is not at its active level.
- A **bus** is a collection of two or more related signal lines.

Binary-to-Decimal Decoder

- The input has n bits
- The output has 2^n bits. Only one bit is asserted at any time.
 - Also known as “1-out-of- m ” (where $m = 2^n$)
- Zero or more EN (enable) lines



4:16 Decoder



Input				Output																
I_3	I_2	I_1	I_0	O_{15}	O_{14}	O_{13}	O_{12}	O_{11}	O_{10}	O_9	O_8	O_7	O_6	O_5	O_4	O_3	O_2	O_1	O_0	
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1
0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	0
0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	0	0	0
0	0	1	1	0	0	0	0	0	0	0	0	0	0	0	0	1	0	0	0	0
0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	1	0	0	0	0	0
0	1	0	1	0	0	0	0	0	0	0	0	0	0	1	0	0	0	0	0	0
0	1	1	0	0	0	0	0	0	0	0	0	0	1	0	0	0	0	0	0	0
0	1	1	1	0	0	0	0	0	0	0	0	1	0	0	0	0	0	0	0	0
1	0	0	0	0	0	0	0	0	0	0	1	0	0	0	0	0	0	0	0	0
1	0	0	1	0	0	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0
1	0	1	0	0	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0
1	0	1	1	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0
1	1	0	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0
1	1	0	1	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0
1	1	1	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
1	1	1	1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0

4:16 Decoder with Active-LOW outputs

Input				Output																
I_3	I_2	I_1	I_0	O_{15_L}	O_{14_L}	O_{13_L}	O_{12_L}	O_{11_L}	O_{10_L}	O_{9_L}	O_{8_L}	O_{7_L}	O_{6_L}	O_{5_L}	O_{4_L}	O_{3_L}	O_{2_L}	O_{1_L}	O_{0_L}	
0	0	0	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0
0	0	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0	1
0	0	1	0	1	1	1	1	1	1	1	1	1	1	1	1	1	0	1	1	1
0	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0	1	1	1	1
0	1	0	0	1	1	1	1	1	1	1	1	1	1	1	0	1	1	1	1	1
0	1	0	1	1	1	1	1	1	1	1	1	1	1	0	1	1	1	1	1	1
0	1	1	0	1	1	1	1	1	1	1	1	1	0	1	1	1	1	1	1	1
0	1	1	1	1	1	1	1	1	1	1	1	0	1	1	1	1	1	1	1	1
1	0	0	0	1	1	1	1	1	1	1	0	1	1	1	1	1	1	1	1	1
1	0	0	1	1	1	1	1	1	1	0	1	1	1	1	1	1	1	1	1	1
1	0	1	0	1	1	1	1	1	0	1	1	1	1	1	1	1	1	1	1	1
1	0	1	1	1	1	1	1	0	1	1	1	1	1	1	1	1	1	1	1	1
1	1	0	0	1	1	1	0	1	1	1	1	1	1	1	1	1	1	1	1	1
1	1	0	1	1	1	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1
1	1	1	0	1	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
1	1	1	1	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1

4:16 Decoder with EN

Input					Output																
EN	I ₃	I ₂	I ₁	I ₀	O ₁₅	O ₁₄	O ₁₃	O ₁₂	O ₁₁	O ₁₀	O ₉	O ₈	O ₇	O ₆	O ₅	O ₄	O ₃	O ₂	O ₁	O ₀	
0	X	X	X	X	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1
1	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	0	0
1	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	0	0	0
1	0	0	1	1	0	0	0	0	0	0	0	0	0	0	0	0	1	0	0	0	0
1	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	1	0	0	0	0	0
1	0	1	0	1	0	0	0	0	0	0	0	0	0	0	1	0	0	0	0	0	0
1	0	1	1	0	0	0	0	0	0	0	0	0	0	1	0	0	0	0	0	0	0
1	0	1	1	1	0	0	0	0	0	0	0	0	1	0	0	0	0	0	0	0	0
1	1	0	0	0	0	0	0	0	0	0	0	1	0	0	0	0	0	0	0	0	0
1	1	0	0	1	0	0	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0
1	1	0	1	0	0	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0
1	1	0	1	1	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0
1	1	1	0	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0
1	1	1	0	1	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0
1	1	1	1	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
1	1	1	1	1	1	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0
1	1	1	1	1	1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0

4:16 Decoder

(Active-HIGH EN)
Active-LOW output

Input					Output																
EN	I ₃	I ₂	I ₁	I ₀	O _{15_L}	O _{14_L}	O _{13_L}	O _{12_L}	O _{11_L}	O _{10_L}	O _{9_L}	O _{8_L}	O _{7_L}	O _{6_L}	O _{5_L}	O _{4_L}	O _{3_L}	O _{2_L}	O _{1_L}	O _{0_L}	
0	X	X	X	X	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
1	0	0	0	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0
1	0	0	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0	1	1
1	0	0	1	0	1	1	1	1	1	1	1	1	1	1	1	1	1	0	1	1	1
1	0	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0	1	1	1	1
1	0	1	0	0	1	1	1	1	1	1	1	1	1	1	1	0	1	1	1	1	1
1	0	1	0	1	1	1	1	1	1	1	1	1	1	1	0	1	1	1	1	1	1
1	0	1	1	0	1	1	1	1	1	1	1	1	1	0	1	1	1	1	1	1	1
1	0	1	1	1	1	1	1	1	1	1	1	1	0	1	1	1	1	1	1	1	1
1	1	0	0	0	1	1	1	1	1	1	1	0	1	1	1	1	1	1	1	1	1
1	1	0	0	1	1	1	1	1	1	1	0	1	1	1	1	1	1	1	1	1	1
1	1	0	1	0	1	1	1	1	1	0	1	1	1	1	1	1	1	1	1	1	1
1	1	0	1	1	1	1	1	1	0	1	1	1	1	1	1	1	1	1	1	1	1
1	1	1	0	0	1	1	1	0	1	1	1	1	1	1	1	1	1	1	1	1	1
1	1	1	0	1	1	1	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1
1	1	1	1	0	1	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
1	1	1	1	1	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1

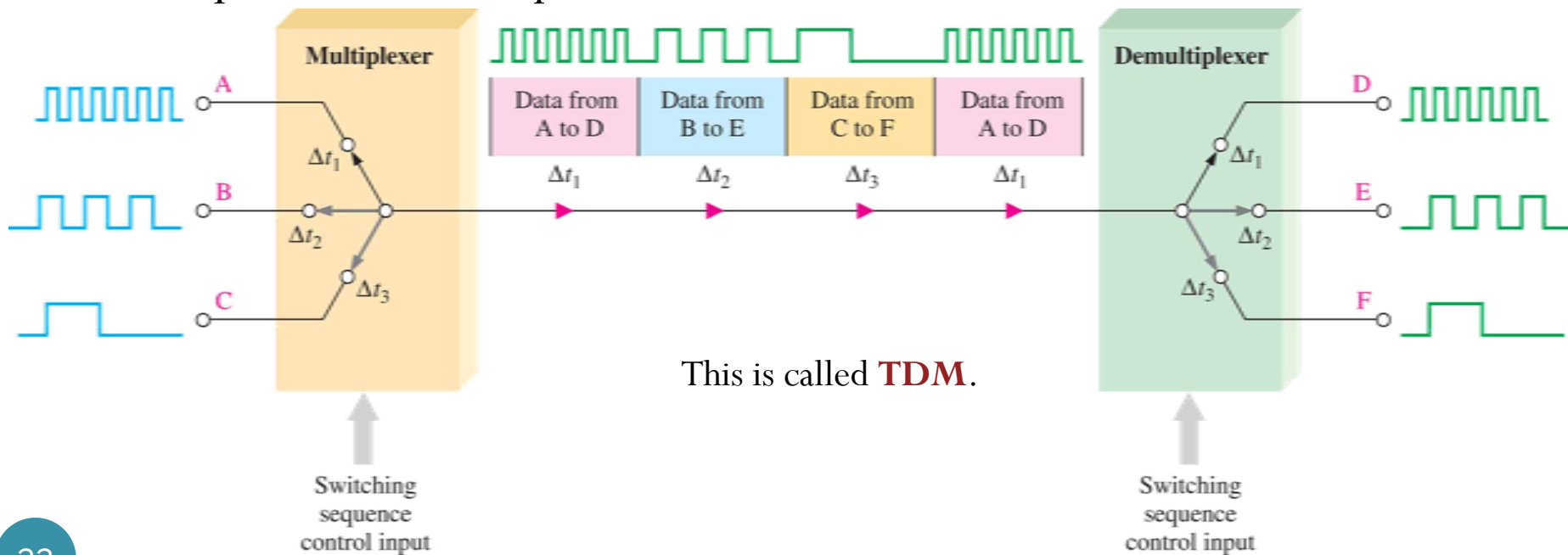
4:16 Decoder

Active-LOW EN
Active-LOW output

Input					Output																
EN_L	I ₃	I ₂	I ₁	I ₀	O _{15_L}	O _{14_L}	O _{13_L}	O _{12_L}	O _{11_L}	O _{10_L}	O _{9_L}	O _{8_L}	O _{7_L}	O _{6_L}	O _{5_L}	O _{4_L}	O _{3_L}	O _{2_L}	O _{1_L}	O _{0_L}	
1	X	X	X	X	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
0	0	0	0	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0
0	0	0	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0	1	1
0	0	0	1	0	1	1	1	1	1	1	1	1	1	1	1	1	0	1	1	1	1
0	0	0	1	1	1	1	1	1	1	1	1	1	1	1	1	0	1	1	1	1	1
0	0	1	0	0	1	1	1	1	1	1	1	1	1	1	1	0	1	1	1	1	1
0	0	1	0	1	1	1	1	1	1	1	1	1	1	0	1	1	1	1	1	1	1
0	0	1	1	0	1	1	1	1	1	1	1	1	0	1	1	1	1	1	1	1	1
0	0	1	1	1	1	1	1	1	1	1	1	0	1	1	1	1	1	1	1	1	1
0	1	0	0	0	1	1	1	1	1	1	1	0	1	1	1	1	1	1	1	1	1
0	1	0	0	1	1	1	1	1	1	1	0	1	1	1	1	1	1	1	1	1	1
0	1	0	1	0	1	1	1	1	1	0	1	1	1	1	1	1	1	1	1	1	1
0	1	0	1	1	1	1	1	1	0	1	1	1	1	1	1	1	1	1	1	1	1
0	1	1	0	0	1	1	1	0	1	1	1	1	1	1	1	1	1	1	1	1	1
0	1	1	0	1	1	1	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1
0	1	1	1	0	1	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
0	1	1	1	1	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1

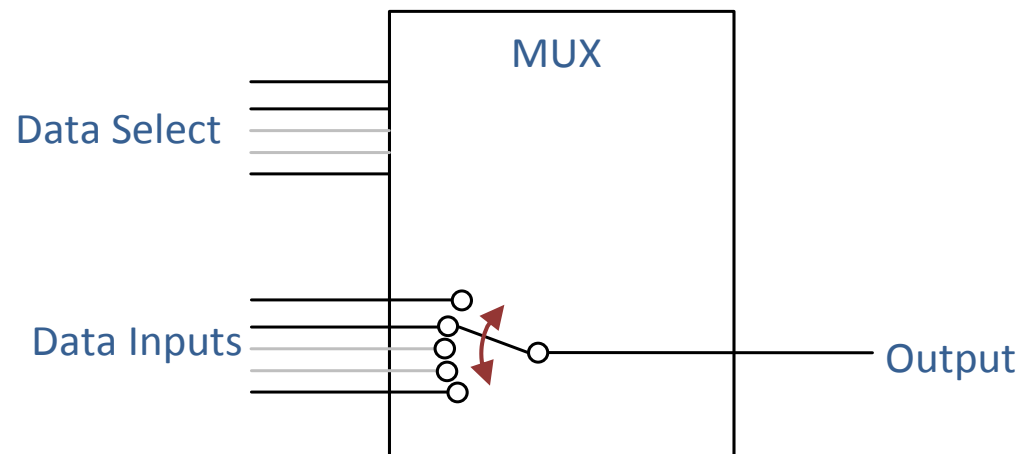
Multiplexing/Demultiplexing

- The **multiplexer**, or **mux** for short, is a logic circuit that switches digital data from several input lines onto a single output line in a specified time sequence.
- The **demultiplexer (demux)** is a logic circuit that switches digital data from one input line to several output lines in a specified time sequence

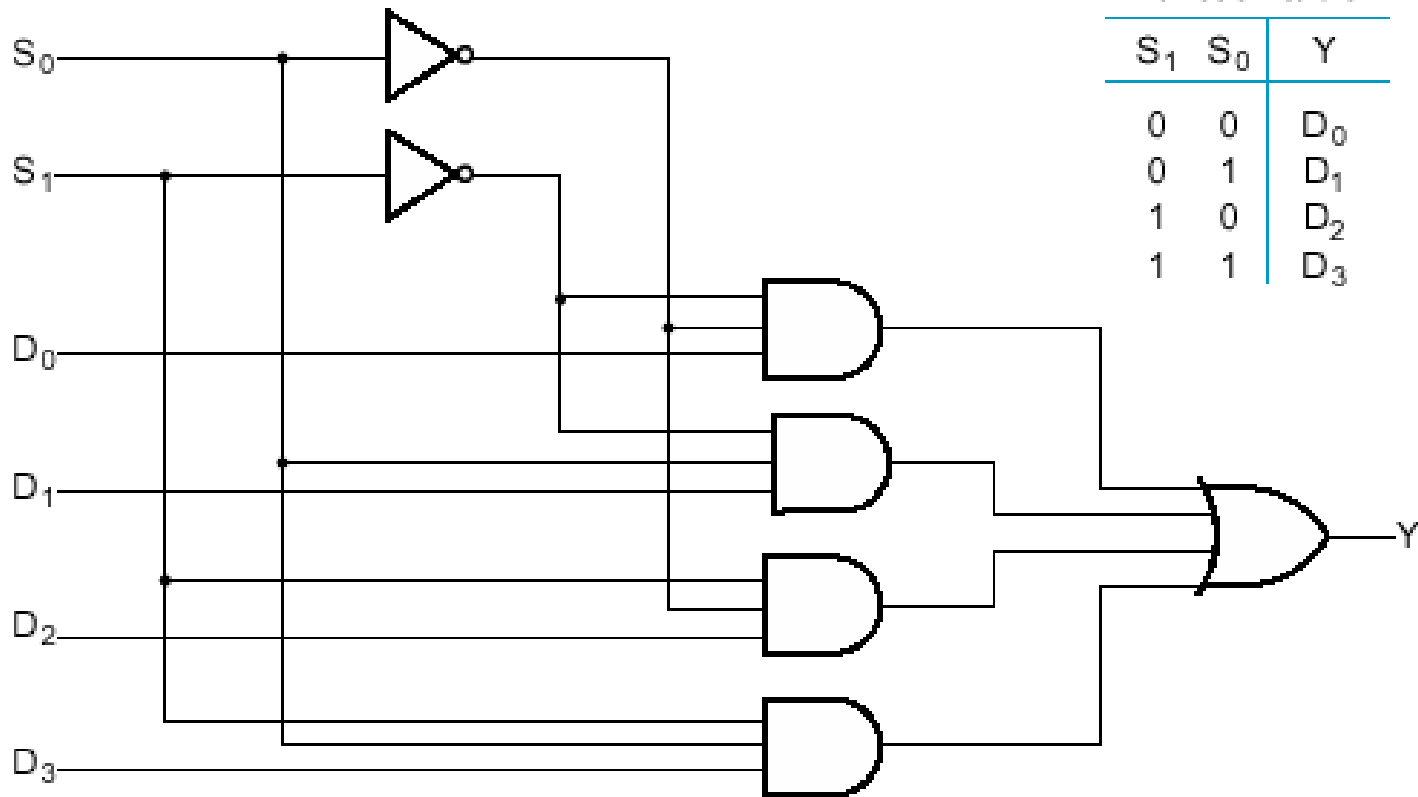


Multiplexer (Data Selector)

- Select binary information from one of many input lines and directs the information to a single output line.
- Allow digital information from several sources to be routed onto a single line for transmission over that line to a common destination.
- Basic multiplexer has
 1. Data-input lines
 2. Single output line.
 3. Data-select inputs



4-to-1-line multiplexer (4:1 MUX)



Example

$$2:1 \text{ mux: } Z = A'I_0 + AI_1$$

$$4:1 \text{ mux: } Z = A'B'I_0 + A'BI_1 + AB'I_2 + ABI_3$$

$$8:1 \text{ mux: } Z = A'B'C'I_0 + A'B'CI_1 + A'BC'I_2 + A'BCI_3 \\ + AB'C'I_4 + AB'CI_5 + ABC'I_6 + ABCI_7$$

